Verifying existence of uniform strategies in systems of communicating agents

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CLAR 2018 Hangzhou

General area of the talk

- This talk is on specification and verification of multi-agent systems (MAS)
- a MAS is specified in terms of states and joint actions by the agents
- actions can change both the physical properties of the state and the knowledge of agents (e.g. observation and communication actions)
- actions consume and produce resources

General area of the talk continued

- verification is done by model checking (checking whether the system satisfies some properties)
- example properties could be:
 - does agent 1 have a strategy to achieve a state where agent 2 always knows/believes that p is true?
 - do agents 1 and 2 have a strategy to come to know whether *p* is true, given their resource allocation?
- in general: is there a strategy for a group of agents to achieve/maintain some property, and what kind of resources are required for this (time, energy, communication costs...)

Background 1: temporal logic and model checking

Temporal logic

temporal logics talk about computational behaviour in state transition systems



• say things like: 'there is a path (run of the system, computation) where in the next state φ holds', 'always φ ', ' φ until ψ '

Temporal logic

- $\bigcirc \varphi$: φ holds in the next state of the path
- $\Box \varphi$: φ holds in every state on the path
- $\varphi \mathcal{U} \psi$: until ψ becomes true, φ holds on the path



Model checking

- represent a computational system as a state transition system
- express properties of interest in temporal logic (e.g. 'does the system deadlock?' ⊤ U deadlock)
- model-checking problem: does a formula φ hold in a state transition system M?
- used in verification of hardware and software for a long time

Alternating time temporal logic

- Alternating-Time Temporal Logic (ATL) is a temporal logic which can talk about groups of agents having a strategy to enforce some outcome (temporal property) whatever the other agents in the system do
- ATL is interpreted over concurrent game structures



Coalitions, (uniform) strategies

- a strategy is a choice of actions (determined by the current state of the agent or by a finite history = sequence of states)
- a coalition is a group of agents, intuitively with a common goal (such as, discover whether *p* is true)
- a coalitions's strategy is *uniform* if every agent in the coalition selects actions based on its knowledge (more on knowledge later; for the moment we consider perfect information)

ATL example

- In *w*₁, agent 1 has a strategy to make sure that in the next state *p*, and after that *p* is true forever (choose *ski*, and after that *null*)
- there is only one computational path generated by this strategy, and in the next state *p* is true
- agent 2 does not have a strategy to enforce p; if it 'chooses' *snow*, agent 1 can perform *ski*, in which case the system is in w_3 , or *drive*, in which case it is in w_2 , where p is false
- there are two paths, and on one of them $\bigcirc p$ does not hold



ATL example

- $M, w_1 \models \langle\!\langle \{1\} \rangle\!\rangle \bigcirc p$
- $M, w_1 \models \langle\!\langle \{1\} \rangle\!\rangle \bigcirc (p \land \langle\!\langle \{1\} \rangle\!\rangle \Box p)$
- $M, w_1 \not\models \langle\!\langle \{2\} \rangle\!\rangle \bigcirc p$



Background 2: epistemic logic

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Standard Epistemic Logic

- standard epistemic logic: agent *a* believes/knows φ (B_aφ/ K_aφ) iff φ is true in all *a*-accessible states
- accessibility relations are the same for all agents in the system; if they are reflexive and transitive, one set of properties for belief/knowledge (S4): all beliefs are consistent, true, and if *a* believes something then it believes that it believes it (positive introspection)
- if accessibility is also symmetric (equivalence relation, often called indistinguishability) then also negative introspection holds (S5)
- what always holds is logical omnisicence: all tautologies are believed, and logical consequences of beliefs are believed

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Example: *a* believes *p* and is agnostic about q_i



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Standard Epistemic Logic

- change of beliefs/knowledge in time:
 - · either attach a set of accessible states to each 'temporal' state
 - or (for knowledge) make the 'local state of the agent' encode the equivalence class for the indistinguishability relation

Syntactic Epistemic Logic

- alternative: in each state, for each agent a, represent a set of formulas a believes or knows
- instead of a set of accessible states, we have a set of formulas
- this set can change as a result of ontic (actions in the world) and epistemic actions

Advantages of Syntactic Epistemic Logic

- more compact models
- different agents can update their beliefs in different ways:
 - upon receiving a message, can incorporate it or ignore it
 - incorporating the content of the message may involve adding it to the knowledge base and closing it under consequence relation in a different logic (S4, S5, or something much weaker)
 - can avoid logical omniscience

Example: *a* believes p and is agnostic about q_i



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Different possibilities for update: ignore the message



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Different possibilities for update: record the fact



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Different possibilities for update: add the content



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Different possibilities for update: add the content and close under inference



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Combination of ATL with resources and epistemics: $RB \pm ATSEL$

- Resource-Bounded Alternating Time Syntactic Epistemic Logic (RB±ATSEL) is designed to reason about resource-bounded agents executing both ontic and epistemic actions
- knowledge is modelled syntactically (as a finite set of formulas: the agent's knowledge base):
 - to avoid the problem of logical omniscience
 - to make modelling epistemic actions manageable

What kind of things can RB±ATSEL express

- 'two robot museum guard robots have a strategy to observe and prevent any attempt approach the artworks in the museum, provided that at least one of them starts fully charged'
- epistemic actions: observing, communicating (anything that changes the agent's knowledge base without changing the world)
- ontic actions: stopping someone from touching an artwork, charging the battery (changing the world)
- resource allocation: the amount of energy each agent has; there can be multiple resource types: energy, memory, etc.

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Concurrent game structure



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Adding resources (one resource type: energy)



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Adding knowledge bases



Strategies

- a strategy for coalition *A* is a mapping from finite sequences of states (histories) to joint actions by agents in *A*
- if *A* is the grand coalition (all agents), any strategy of *A* generates a single run of the system
- otherwise, a strategy corresponds to a tree (each branch of the tree is a run corresponding to a particular choice of actions by A's opponents)
- strategies possible given a particular resource allocation b: a strategy is a b-strategy if for every run generated by this strategy, for each action by A in the strategy, the agents in A will have enough resources to execute it

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Language of RB±ATSEL

- In what follows, we assume a set Agt = {a₁,..., a_n} of n agents, Res = {res₁,..., res_r} a set of r resource types, and a set of propositions Π
- The set of possible resource bounds or resource allocations is $B = Agt \times Res \rightarrow \mathbb{N}_{\infty}$, where $\mathbb{N}_{\infty} = \mathbb{N} \cup \{\infty\}$.
- Formulas of the language ${\cal L}$ of RB±ATSEL are defined by the following syntax

 $\varphi ::= p \mid \neg \varphi \mid \varphi \lor \psi \mid \langle\!\langle \mathbf{A}^{\mathbf{b}} \rangle\!\rangle \bigcirc \varphi \mid \langle\!\langle \mathbf{A}^{\mathbf{b}} \rangle\!\rangle \varphi \mathcal{U} \psi \mid \langle\!\langle \mathbf{A}^{\mathbf{b}} \rangle\!\rangle \Box \varphi \mid \mathbf{K}_{\mathbf{a}} \varphi$

where $p \in \Pi$ is a proposition, $A \subseteq Agt$, $b \in B$ is a resource bound and $a \in Agt$.

Meaning of formulas

- ((A^b))ψ₁ U ψ₂ means that A has a strategy executable within resource bound b to ensure ψ₂ while maintaining the truth of ψ₁
- ((A^b))□ψ means that A has a strategy executable within resource bound b to ensure that ψ is always true
- *K_aφ* means that formula *φ* is in agent *a*'s knowledge base. Note that this is a syntactic knowledge definition.

What kind of things can RB±ATSEL express

• if something bad happens (approaching the artwork), one of the guards will know in the next state, provided one of them has one unit of energy:

$$\langle\!\langle \{a_1, a_2\}^{1,0} \rangle\!\rangle \Box$$
(bad $\rightarrow \langle\!\langle \{a_1, a_2\}^{0,0} \rangle\!\rangle \bigcirc (K_{a_1}$ bad $\lor K_{a_2}$ bad))

Models of RB±ATSEL

A model of RB±ATSEL is a structure $M = (\Phi, Agt, Res, S, \Pi, Act, d, c, \delta)$ where:

- Φ is a finite set of formulas of L (possible contents of the local states of the agents).
- S is a set of tuples (s₁,..., s_n, s_e) where s_e ⊆ Π and for each a ∈ Agt, s_a ⊆ Φ.
- Agt, Res, П are as before
- Act is a non-empty set of actions which includes *idle*, and $d: S \times Agt \rightarrow \wp(Act) \setminus \{\emptyset\}$ is a function which assigns to each $s \in S$ a non-empty set of actions available to each agent $a \in Agt$. We assume that for every $s \in S$ and $a \in Agt$, *idle* $\in d(s, a)$. We denote joint actions by all agents in Agt available at s by $D(s) = d(s, a_1) \times \cdots \times d(s, a_n)$.

Models continued

- for every $s, s' \in S, a \in Agt, d(s, a) = d(s', a)$ if $s_a = s'_a$.
- c: Act × Res → Z is the function which models consumption and production of resources by actions (a positive integer means consumption, a negative one production).
- $\delta: S \times Act^n \to S$ is a partial function which for every $s \in S$ and joint action $\sigma \in D(s)$ returns the state resulting from executing σ in *s*.

Costs of strategies

 A strategy is a *b*-strategy (can be carried out under resource bound *b*) if every computation for this strategy can be carried out with initial resource allocation *b* (resources of agents will never drop below 0).

Uniform strategies

- a strategy is uniform if, after epistemically indistinguishable histories, agents select the same actions
- two states *s* and *t* are epistemically indistinguishable by agent *a*, denoted by $s \sim_a t$, if *a* has the same local state (knows the same formulas) in *s* and *t*: $s \sim_a t$ iff $s_a = t_a$
- \sim_a can be lifted to sequences of states in an obvious way
- a strategy for A is uniform if it is uniform for every agent in A

Coalition uniform strategies

- for a coalition A, indistinguishability s ∼_A s' means that A as a whole has the same knowledge in the two states
- various notions of coalitional knowledge can be used to define ~_A, for example:
 - $s \sim_A t$ iff $\bigcup_{a \in A} s_a = \bigcup_{a \in A} t_a$ (the distributed knowledge of A in s and t is the same)
 - another possible definition of $s \sim_A t$ is $\forall a \in A(s_a = t_a)$
- a strategy for A is coalition uniform with respect to \sim_A if it assigns agents in A the same actions in any two histories indistinguishable in \sim_A

Truth definition

- $M, s \models p$ iff $p \in s_e$
- boolean connectives have standard truth definitions
- *M*, *s* ⊨ ⟨⟨*A^b*⟩⟩ ⊖ φ iff ∃ coalition-uniform *b*-strategy *F_A* such that for all λ ∈ out(*s*, *F_A*): *M*, λ[1] ⊨ φ
- $M, s \models \langle\!\langle A^b \rangle\!\rangle \phi \mathcal{U} \psi$ iff \exists coalition-uniform *b*-strategy F_A such that for all $\lambda \in out(s, F_A)$, $\exists i \ge 0$: $M, \lambda[i] \models \psi$ and $M, \lambda[j] \models \phi$ for all $j \in \{0, \dots, i-1\}$
- *M*, *s* ⊨ ⟨⟨*A^b*⟩⟩□φ iff ∃ coalition-uniform *b*-strategy *F_A* such that for all λ ∈ *out*(*s*, *F_A*) and *i* ≥ 0: *M*, λ[*i*] ⊨ φ.
- $M, s \models K_a \phi$ iff $\phi \in s_a$

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Syntactic definition for K_a

- $M, s \models K_a \phi$ iff $\phi \in s_a$: *a* knows ϕ iff ϕ is in *a*'s state
- more general definition: let alg_a be any algorithmic (terminating) procedure that produces *a*'s knowledge when applied to s_a
- for example, *alg_a* could be computing the largest subset of some finite set of formulas that is derivable from *s_a* in a particular logic

Model-checking problem for RB±ATSEL

- given a model *M* of RB±ATSEL and a RB±ATSEL formula ϕ , return the set of states of *M* where ϕ is true
- the model-checking problem for ATL with perfect recall and uniform strategies is undecidable (because RB±ATSEL is an extension of ATL with perfect recall)
- The model-checking problem for RB±ATSEL with coalition-uniform strategies, with respect to any decidable notion of ∼_A, is decidable [IJCAI 2016].

Adding explicit communication step

- coalition uniformity presupposes that agents can select actions based on the knowledge of other agents in the coalition
- to make this assumption realistic, we add an explicit communication step, with associated costs

Original model (fragment)



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Communication model (fragment)



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Communication models

main points:

- two disjoints sets of states, action states and communication states
- in action states, only communication actions of the form *com*(*X*, *A*) where *X* ⊆ *s_a* (send some contents of state of *a* to all agents in *A*) are available
- the effect of communication action is adding communicated formulas *X* to the state of every agent in *A*
- we changed the truth definition of 'next' for communication states (to look two steps ahead)

Model checking for communication models

- Model checking RB±ATSEL over communication models is decidable for perfect recall uniform strategies
- model checking algorithm is obtained by modifying the algorithm for RB±ATSEL for coalition-uniform strategies (for the special case where ~_A is equivalence of recently communicated formulas)
- the algorithm has an added check for the type of each state that is encountered in the search
- in action states, each agent a ∈ A executes com(X, A), X ⊆ s_a required by communication protocol ρ, which results in a state where all agents in A have the same recently communicated information
- the choice of com(X, A) results in a uniform strategy because each agent in A always communicates the same information to other agents in A required by the knowledge-based protocol

The cost of communication

• The *com*(*X*, *A*) action can be assigned a cost based e.g., on the number of agents in *A* and the number of formulas in *X*

Conclusions

- the model-checking problem for ATL with uniform strategies and perfect recall is undecidable
- however, it is decidable for strategies uniform with respect to e.g., distributed knowledge of the whole coalition
- it is also decidable in models where agents can communicate (following a fixed knowledge-based communication protocol) before action selection

Thank you! Questions?

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